

# ON CERTAIN ORDER ON IDEALS AND ON RELATED CARDINAL COEFFICIENTS

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**Abstract:** We present cardinal coefficients connected to a natural partial order on the family of ideals on  $\omega$ . These new coefficients are natural generalizations of the pseudo-intersection number  $\mathfrak{p}$ . We show consistency of some inequalities of these coefficients and classical ones, and other related combinatorial questions. Furthermore, we discuss ideals generated by almost disjoint families and towers, and we analyze related maximality properties of these families. We give some analytic motivations for the considered problems connected to sequential properties of spaces of measures with weak\* topology.

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