

Price Risk Based Power Portfolio Optimization with Liquidity Constraints

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Power as a product

Electricity cannot be stored:

- ▶ Production and consumption have to be equal.

Demand side:

- ▶ Short-term demand is inelastic.
- ▶ The future demand/consumption is uncertain.

Supply side:

- ▶ Given power plant capacity.
- ▶ Transportability, infrastructure constraints.
- ▶ Solar and wind power production uncertainties,
- ▶ power plant outages.

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Power related markets

Wholesale electricity market

The traded product is electricity

- ▶ for a given time period,
- ▶ with a given power level for each (quarter) hour,
- ▶ sometimes with some tolerance.

Capacity market

- ▶ Cross-border capacities.

Regulation power market

- ▶ Balancing energy.
- ▶ Control power market.

Transmission System fees

- ▶ Transmission system operation fee.
- ▶ Charges for ancillary services.
- ▶ Distribution charges.

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Standard power products

Spot market (day-ahead/ $D - 1$)

- ▶ hourly and block products.

Intraday market (D)

- ▶ hourly products.

Derivatives market

- ▶ futures (standard forward products),
- ▶ options (typically on futures with different expiries).

Typical profiles of standard products

- ▶ base-load: 0-24, all days,
- ▶ peak-load: 8-20, Mo-Fr,
- ▶ off-peak: complementary of peak-load.

Typical maturities of standard products

- ▶ day, week, month, quarter, year

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OTC markets



Hungarian Power

Trader in Focus:




Wed 24/04/2013	Hungary Baseload							Hungary Peak (08-20)						
	Code	Qty	Bid	Ask	Qty	Code	Last	Code	Qty	Bid	Ask	Qty	Code	Last
Thu 25/04/2013							32,50							
Fri 26/04/2013		10	28,00	34,00	10									
Sat 27/04/2013														
Sun 28/04/2013														
Mon 29/04/2013		10	33,10	36,00	10		33,90							
Tue 30/04/2013		10	29,50	38,75	10									
WkEnd 27/4-28/		25*	23,50	24,00	10									
WkEnd 4/5-5/														
Wk18 29/04/13		5	28,40	29,25	10		29,75							
Wk19 06/05/13		10	28,10	32,25	10									
Wk20 13/05/13		10	34,25	36,25	5									
Wk 18-13 (WD)														
Wk 19-13 (WD)														
Bal of Month														
May-13		10	33,75	34,20	10		33,80		5	40,75	41,75	5		41,00
Jun-13		10	36,50	37,25	5		37,00		10	44,75	47,50	10		
Jul-13		10	40,50	44,00	5									
Aug-13		10	42,00	49,00	10									
Sep-13		10	43,00	49,00	10									
Oct-13														

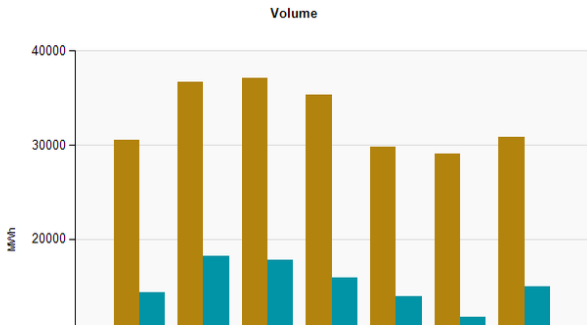
Hungarian Power Exchange (HUPX)

> MARKET DATA ↕

HUPX DAM | HUPX PhF Please enter the code ↻ OK

ATC values | **Weekly data** | Data Chart | Aggregated | MC results

Delivery day: 27/10/2014 Report Type   



> HUPX DAM ↕

Delivery day: 28/10/2014

Price Base (€/MWh): 56.26 ▲
 Price Peak (€/MWh): 72.60 ▲
 Vol. Day (MWh): 28,891.5 ▼
 Vol. Month (MWh): 952,563.5

ATC values | Delivery day: 29/10/2014
[Read more >](#)

> HUPX PhF ↕

	base		peak	
	price (€/MWh)	volume (lot)	price (€/MWh)	volume (lot)
Wk45-14	47.87 ▼		N/A	
Wk46-14	44.00 ▼		N/A	
Wk47-14	44.67 ▼		N/A	
Wk48-14	45.00 ▼		N/A	
Nov-14	44.63 ▼		55.44 ▼	
Dec-14	43.40 ▼	5	53.26 ▼	
Jan-15	46.25 ▼		55.36 ▼	
Q1-15	45.42 ▼	5	55.61 ▼	
Q2-15	37.70 ▼		45.89 ▲	
Q3-15	43.73 ▼		53.13 ▲	
Q4-15	44.55 ▲		53.86 ▲	
YR-15	42.85 ▼	10	52.12 ▲	
YR-16	42.79 ▼		52.25 ▼	
YR-17	42.80 ▼		52.02 ▼	

European Energy Exchange (EEX)



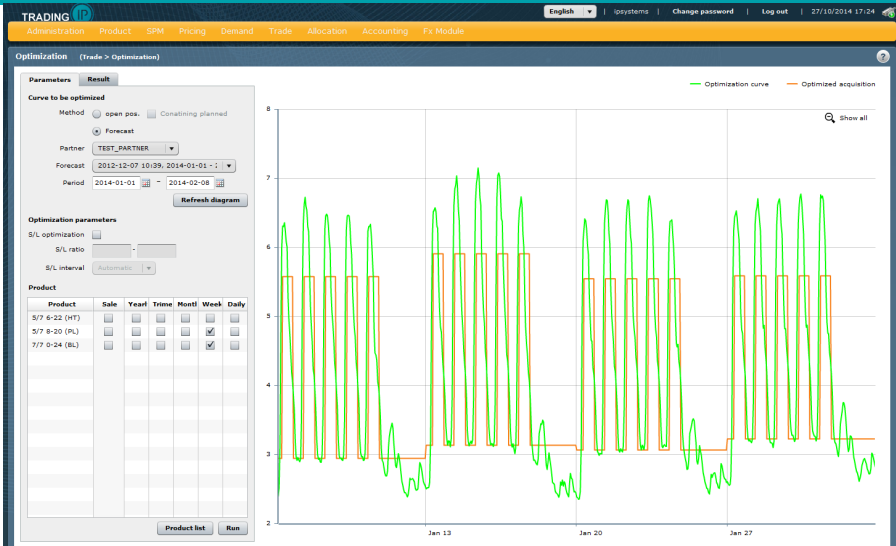
- Products
- Trading
- Market Data
- Access
- Training

Power Products offered at EEX

	Products	Contracts
Spot market 24/7	<ul style="list-style-type: none"> · Day-Ahead Auction (CH) · Day-Ahead Auction (DE/AT, FR) · Intraday (DE, AT, FR, CH) 	Day-ahead market <ul style="list-style-type: none"> · Hour and block contracts (DE/AT, FR, CH) Intraday market <ul style="list-style-type: none"> · Hour and block contracts (DE/AT, FR) · 15-minute contracts (DE/AT, CH)
Derivatives Market	<ul style="list-style-type: none"> · Phelix-Futures (DE/AT) 	<ul style="list-style-type: none"> · Day Futures



Volume-based hedging



Expected value vs. Risk: St. Petersburg paradox

(de Montmort 1713, Bernoulli 1738)

A casino offers a game of chance in which a fair coin is tossed at each stage.

- ▶ The pot starts at 2 dollars,
- ▶ and is doubled every time a head appears.

What would be the fair price of the game?

Consider, the expected value of the payout:

$$\begin{aligned}
 E(\text{Payout}) &= \frac{1}{2} \cdot 2 + \frac{1}{2^2} \cdot 2^2 + \frac{1}{2^3} \cdot 2^3 + \dots \\
 &= 1 + 1 + 1 + \dots = \infty
 \end{aligned}$$

Hence, selling all your wealth, then paying all the money to the casino to enter the game seems to be a reasonable choice! (?)

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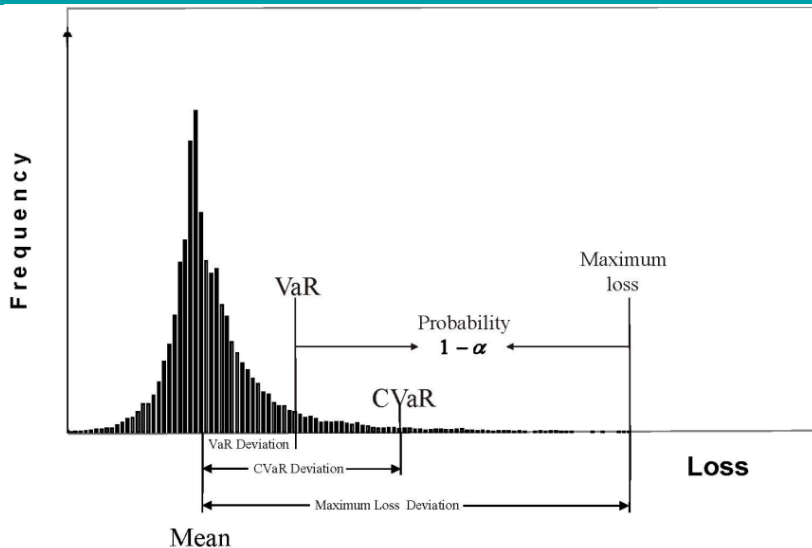
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(Conditional) Value-at-Risk



Exact definition of (Conditional) Value-at-Risk

Let the random loss denoted by L and the level of significance denoted by $0 < \alpha < 1$.

Definition (Value-at-Risk)

$$\text{VaR}_\alpha(L) = \min \{z \mid F_L(z) \geq \alpha\}.$$

Definition (Conditional Value-at-Risk)

$$\text{CVaR}_\alpha(L) = \int_{-\infty}^{+\infty} z dF_L^\alpha(z),$$

where

$$F_L^\alpha(z) = \begin{cases} 0, & \text{if } z < \text{VaR}_\alpha(L) \\ \frac{F_L(z) - \alpha}{1 - \alpha}, & \text{if } z \geq \text{VaR}_\alpha(L) \end{cases}$$

Calculation of Conditional Value-at-Risk

Definition (Upper Conditional Value-at-Risk)

$$CVaR_{\alpha}^{+}(L) = E [L | L > VaR_{\alpha}(L)].$$

Also called Mean Excess Loss and Expeced Shortfall.

Definition (Lower Conditional Value-at-Risk)

$$CVaR_{\alpha}^{-}(L) = E [L | L \geq VaR_{\alpha}(L)].$$

Also called TailVaR.

Theorem

$$CVaR_{\alpha}(L) = \begin{cases} \lambda_{\alpha}(L) VaR_{\alpha}(L) + (1 - \lambda_{\alpha}(L)) CVaR^{+}(L), & F_L(VaR_{\alpha}(L)) < 1 \\ VaR_{\alpha}(L), & F_L(VaR_{\alpha}(L)) = 1, \end{cases}$$

where

$$\lambda_{\alpha}(L) = \frac{F_L(VaR_{\alpha}(L)) - \alpha}{1 - \alpha}$$

Properties of CVaR

The major innovation of the definition of CVaR:

- ▶ CVaR is continuous with respect to L ,
- ▶ CVaR is convex in L .

Some remarks:

- ▶ VaR, $CVaR^-$, $CVaR^+$ may be non-convex
- ▶ $VaR \leq CVaR^- \leq CVaR \leq CVaR^+$

CVaR is a coherent risk measure. If A and B are two portfolios, then

1. $CVaR(\emptyset) = 0$,
2. if $A \leq B$ then $CVaR(A) \leq CVaR(B)$,
3. $CVaR(x \cdot A) = x \cdot CVaR(A)$,
4. $CVaR(A + x) = CVaR(A) - x$, where x is cash (constant),
5. $CVaR(A + B) \leq CVaR(A) + CVaR(B)$, subadditivity.

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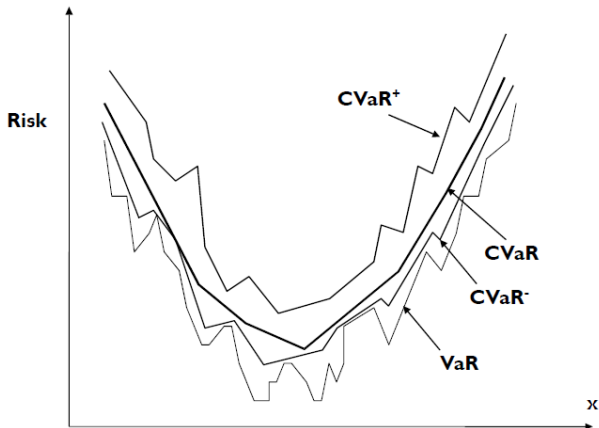
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Convexity of CVaR



Rockafellar, R.T. and S. Uryasev (2000). Optimization of conditional value-at-risk. *Journal of Risk* 2, 21–41.

Planning and holding periods

There is a planning horizon, typically more than one year.

The portfolio consists of

- ▶ an aggregate net demand curve,
- ▶ and long and short positions of standard forward products.

Each product as well as the demand curve must be within the planning horizon.

There is a holding period, typically 2 weeks.

- ▶ The portfolio cannot be re-hedged within the holding period.
- ▶ Hence, the (re-)hedging occurs at the beginning of the holding period
- ▶ and we focus on the changes in the portfolio value during the holding period.

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Mark-to-Market (MtM)

Each ingredient of the portfolio can be valued in the following way.

- ▶ In case of standard forward products:
 - ▶ if the product has price on the market, then that should be used,
 - ▶ if there is no contract on the product, then some consistent market-based approximation can be used.
- ▶ The aggregate net demand curve can be valued by the so-called Hourly Price Forward Curve (HPFC).
 - ▶ The HPFC gives forecast for the price of each hourly spot product.
 - ▶ The value of the net demand curve is simply the scalar product of the demand curve quantities and price curve prices.

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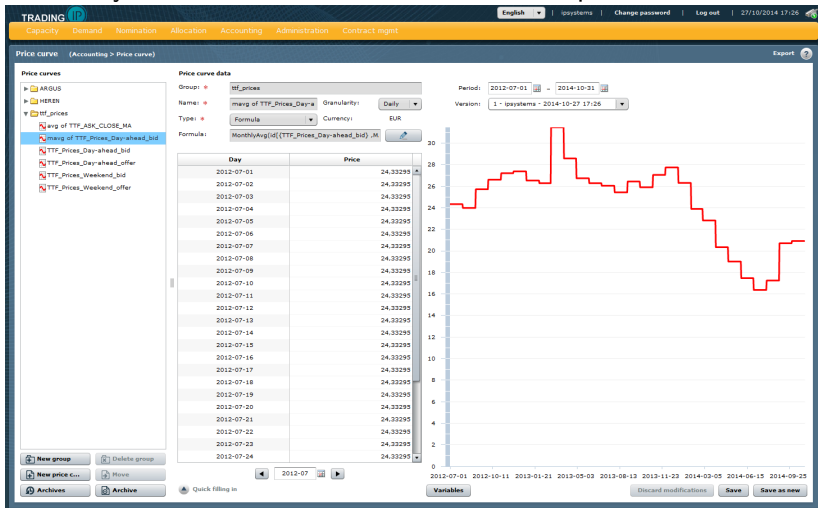
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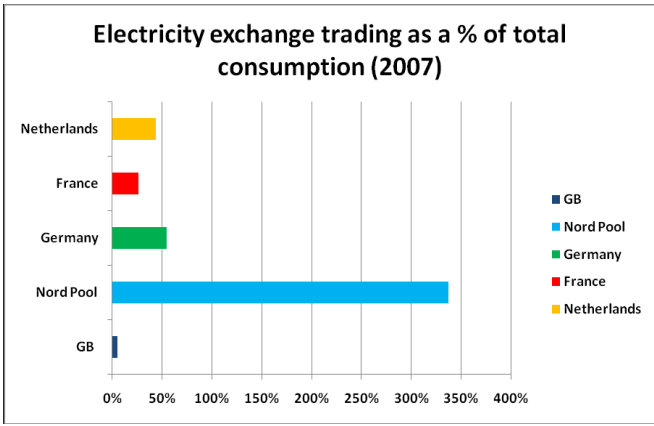
Price curves

Electricity is non-storable: it has different unit price for each hour.



The market: Liquidity

The liquidity of wholesale energy markets is very poor.



The main reasons are: vertical integration, a lack of interconnection, imbalance prices, collateral requirements.

(C)VaR vs. (C)PaR

The valuation of a portfolio is splitted into two parts.

- ▶ The liquid part of the portfolio
 - ▶ consists of the positions that can be closed on the market immediately.
 - ▶ The subportfolio can be valued by forward prices.
- ▶ The illiquid part of the portfolio
 - ▶ consists of the remainder positions that cannot be closed because of the market illiquidity.
 - ▶ The subportfolio can be valued by HPFC.

The "business" terms

- ▶ (Conditional) Profit-at-Risk means the "mathematical" (C)VaR value of the illiquid part of the portfolio.
- ▶ (Conditional) Value-at-Risk means the (C)VaR value of positions that can be closed.

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The problem: Input

- ▶ Initial portfolio: net demand curve and forward products,
- ▶ the holding period,
 - ▶ at the beginning of the holding period:
 - ▶ available forward products with their liquidity bounds,
 - ▶ prices of the forward products,
 - ▶ HPFC.
 - ▶ For the end of the holding period:
 - ▶ available forward products with their liquidity bounds,
 - ▶ scenarios:
 - ▶ for the price of the forward products,
 - ▶ for the HPFC.

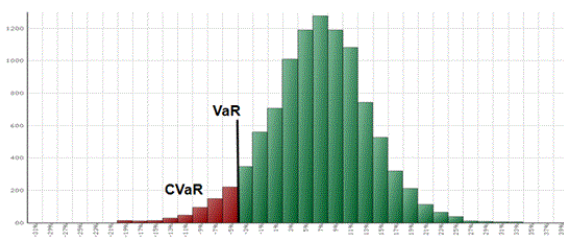
The problem: Objective

- ▶ Let us calculate the changes in value of the hedged portfolio for each scenario.
- ▶ The changes in value is a profit-type quantity. Profit=-Loss. Hence, the profit based CVaR can be calculated from the portfolios.

- ▶ Our aim is to find the hedging strategy (i.e., forward product trading strategy at the beginning of the holding period), which optimize the CVaR value.

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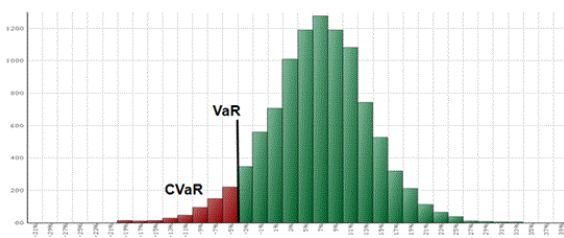
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Alternative definition of CVaR

Pflug, G. C. (2000). Some remarks on the value-at-risk and the conditional value-at-risk. In Probabilistic constrained optimization (pp. 272-281). Springer US.

$$CVaR_{\alpha}(L) = \min_v \left\{ v + \frac{1}{1 - \alpha} E[L - v]^+ \right\}$$

$$VaR_{\alpha}(L) = \arg \min_v \left\{ v + \frac{1}{1 - \alpha} E[L - v]^+ \right\}$$

Optimization of CVaR

- ▶ Define the loss function

$$L = f(\mathbf{x}, \mathbf{Y}),$$

where \mathbf{x} is the decision vector and \mathbf{Y} is a random vector.



$$F_{\alpha}(\mathbf{x}, v) := v + \frac{1}{1 - \alpha} E ([f(\mathbf{x}, \mathbf{Y}) - v]^+)$$

- ▶ Then

$$CVaR_{\alpha}(f(\mathbf{x}, \mathbf{Y})) = \min_v F_{\alpha}(\mathbf{x}, v).$$

- ▶ Hence,

$$\min_{\mathbf{x}} CVaR_{\alpha}(L) = \min_{(\mathbf{x}, v)} F_{\alpha}(\mathbf{x}, v)$$

Optimization based on scenarios

Discrete distribution:

$$P(\mathbf{Y} = \mathbf{y}^i) = p_i, \quad i = 1, \dots, l.$$

Then:

$$F_\alpha(\mathbf{x}, v) = v + \frac{1}{1-\alpha} \sum_{i=1}^l [f(\mathbf{x}, \mathbf{y}^i) - v]^+$$

Hence, the the CVaR minimization can be formulated as

$$\begin{aligned} \min_{(\mathbf{x}, v)} \quad & v + \frac{1}{1-\alpha} \sum_{i=1}^l p_i z_i \\ \text{subject to} \quad & \\ f(\mathbf{x}, \mathbf{y}^i) - v & \leq z_i, \quad i = 1, \dots, l \\ z_i & \geq 0. \end{aligned}$$

Liquidity constraints

- ▶ y_{f0}^{r-} : binary variable that equals 1 iff the short position product f cannot be closed entirely,
- ▶ y_{f0}^{c+} : binary variable that equals 1 iff the long position product f can be closed entirely,
- ▶ pos_{ft}^{c-} : absolute value of the short position of product f if the position can be closed entirely
- ▶ pos_{ft}^{r+} : absolute value of the long position of product f if the position can be closed entirely

Value of the liquid and illiquid subportfolio, respectively:

$$cv_0 = \sum_{f=1}^{FP} (-U_{f0}y_{f0}^{r-} - pos_{f0}^{c-} + pos_{f0}^{c+} + L_{f0}y_{f0}^{r+}) P_{f0}$$

$$rv_0 = \sum_{f=1}^{FP} (-pos_{f0}^{r-} + U_{f0}y_{f0}^{r-} + pos_{f0}^{r+} - L_{f0}y_{f0}^{r+}) R_{f0} - R_{LC0}$$

The objective function

$$\max CVaR_{\alpha}(cv_H + rv_H - cv_0 - rv_0)$$

Linear objective function:

$$\max \left(-v + \sum_{i=1}^I -\frac{1}{I(1-\alpha)} z^i \right)$$

subject to

$$-cv_H^i - rv_H^i + cv_0 + rv_0 - v \leq z^i, \quad i \in \{1, \dots, I\}$$

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subject to

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Multiple optima

Minimizing the number (cost) of transactions. E.g., do not buy Jan, Feb, Mar products instead of Q1.

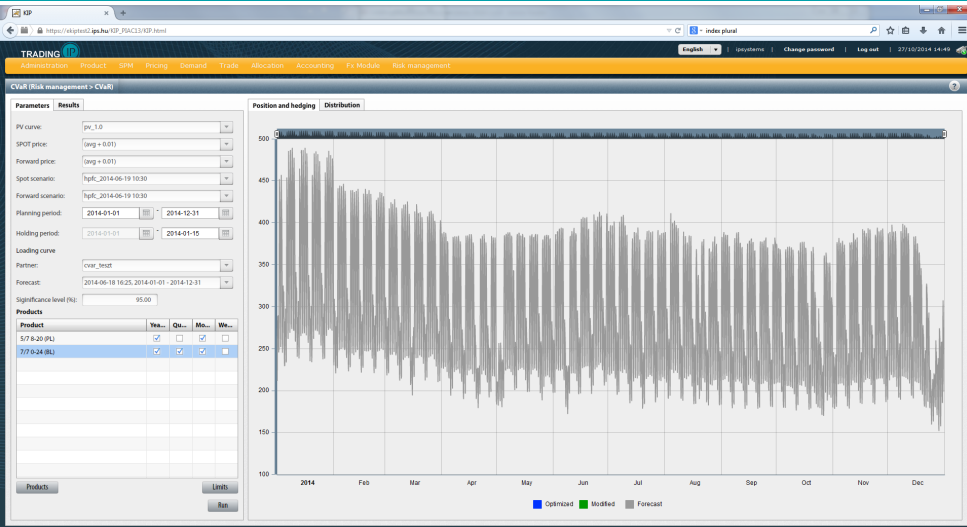
$$\min \sum_{f=1}^{FP} (x_f^- + x_f^+)$$

subject to

$$\begin{aligned} x_f &\leq x_f^+, & f &\in \{1, \dots, FP\} \\ -x_f &\leq x_f^-, & f &\in \{1, \dots, FP\} \end{aligned}$$

$$\left(-v - \frac{1}{l(1-\alpha)} \sum_{i=1}^l z^i \right) \geq CVaR_{opt}$$

Input data



The screenshot shows a web-based trading application interface. The browser address bar displays 'https://ekiprest02.ips.hu/KIP_PJAC13/KIP.html'. The application header includes 'TRADING IP' and navigation tabs for Administration, Product, SPM, Pricing, Demand, Trade, Allocation, Accounting, FX Module, and Risk management. The main content area is titled 'CVaR (Risk management > CVaR)' and is split into two panes.

Parameters pane:

- PV curve: pv_1.0
- SPOT price: (avg + 0.01)
- Forward price: (avg + 0.01)
- Spot scenario: hpfic_2014-06-19 10:30
- Forward scenario: hpfic_2014-06-19 10:30
- Planning period: 2014-01-01 to 2014-12-31
- Holding period: 2014-01-01 to 2014-01-15
- Loading curve: cva_rtest
- Forecast: 2014-06-18 16:25, 2014-01-01 - 2014-12-31
- Significance level (k): 95.00

Products table:

Product	Yes...	Qu...	Ma...	W...
5/7 8-20 (PL)	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>
7/7 0-24 (BL)	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>

Position and hedging chart:

The chart displays a time series of values from January 2014 to December 2014. The y-axis ranges from 100 to 500. The data shows high volatility, with values fluctuating between approximately 150 and 500. A legend at the bottom indicates three data series: Optimized (blue square), Modified (green square), and Forecast (grey square). The chart area is filled with a dense grey line representing the forecast data.

Input data

Parameters
Results

PV curve:

SPOT price:

Forward price:

Spot scenario:

Forward scenario:

Planning period: -

Holding period: -

Loading curve

Partner:

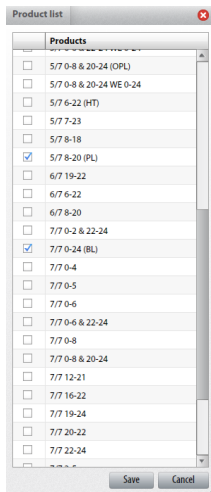
Forecast:

Significance level (%):

Products

Product	Yea...	Qu...	Mo...	We...
5/7 8-20 (PL)	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>
7/7 0-24 (BL)	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>

Product types



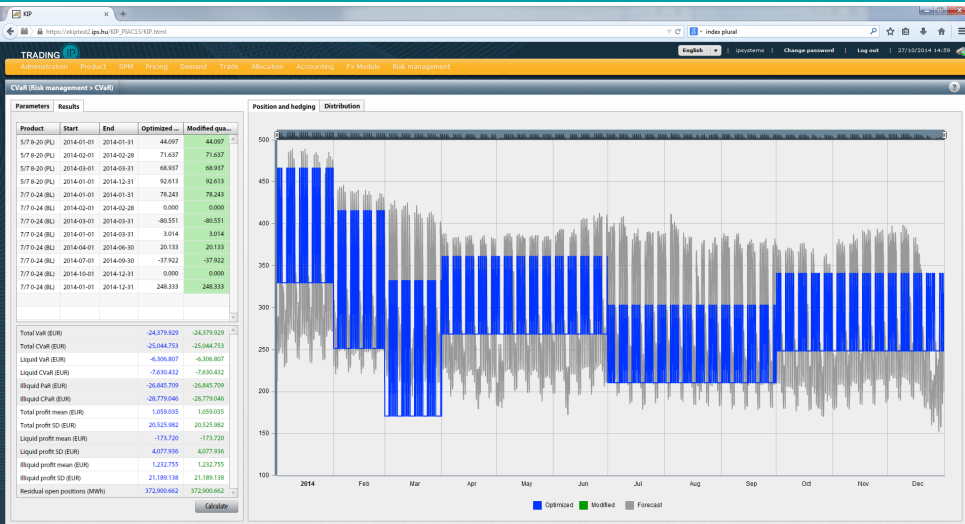
Liquidity limits and initial positions

Limits

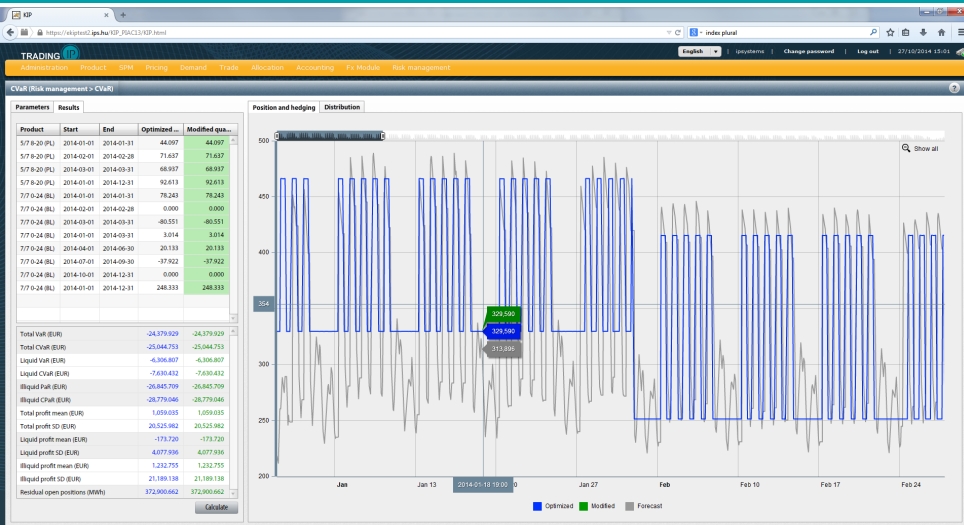
Products	Period	Start	End	Position	Trading limit - lower	Trading limit - top	Closing limit T0 - lower	Closing limit T0 - top	Closing limit TH - lower	Closing limit TH - top
5/7 8-20 (PL)	M1	2014-01-01	2014-01-31	0	1,000	1,000	1,000	1,000	0	0
5/7 8-20 (PL)	M2	2014-02-01	2014-02-28	0	1,000	1,000	1,000	1,000	0	0
5/7 8-20 (PL)	M3	2014-03-01	2014-03-31	0	500	100	500	100	550	150
5/7 8-20 (PL)	Y1	2014-01-01	2014-12-31	0	1,000	1,000	1,000	1,000	0	0
7/7 0-24 (BL)	M1	2014-01-01	2014-01-31	0	1,000	1,000	1,000	1,000	0	0
7/7 0-24 (BL)	M2	2014-02-01	2014-02-28	0	1,000	1,000	1,000	1,000	0	0
7/7 0-24 (BL)	M3	2014-03-01	2014-03-31	0	1,000	1,000	1,000	1,000	0	0
7/7 0-24 (BL)	Q1	2014-01-01	2014-03-31	0	1,000	1,000	1,000	1,000	0	0
7/7 0-24 (BL)	Q2	2014-04-01	2014-06-30	0	1,000	1,000	1,000	1,000	0	0
7/7 0-24 (BL)	Q3	2014-07-01	2014-09-30	0	1,000	1,000	1,000	1,000	0	0
7/7 0-24 (BL)	Q4	2014-10-01	2014-12-31	0	1,000	1,000	1,000	1,000	0	0
7/7 0-24 (BL)	Y1	2014-01-01	2014-12-31	0	1,000	1,000	1,000	1,000	0	0

Save Cancel

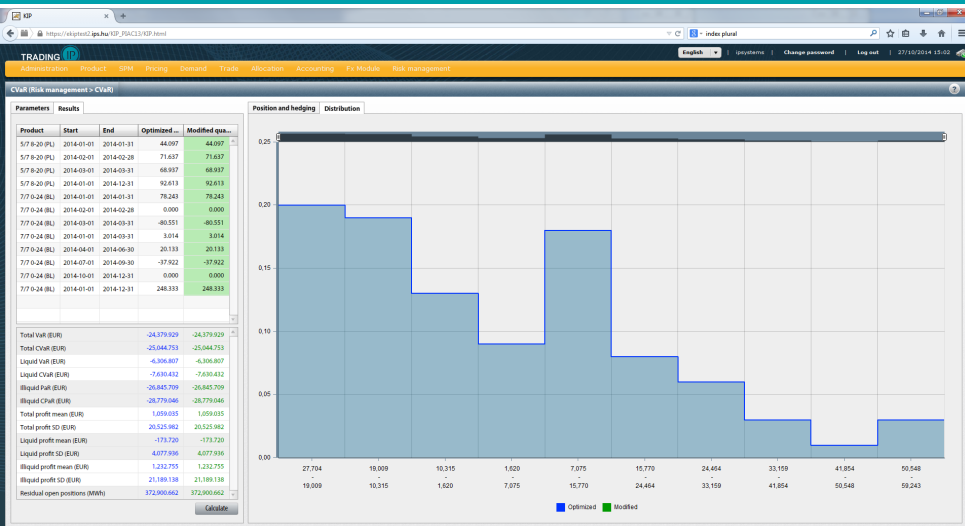
Results



Results



Profit histogram



Modification

Parameters		Results		
Product	Start	End	Optimized ...	Modified qua...
5/7 8-20 (PL)	2014-01-01	2014-01-31	44.097	44.097
5/7 8-20 (PL)	2014-02-01	2014-02-28	71.637	71.637
5/7 8-20 (PL)	2014-03-01	2014-03-31	68.937	68.937
5/7 8-20 (PL)	2014-01-01	2014-12-31	92.613	92.613
7/7 0-24 (BL)	2014-01-01	2014-01-31	78.243	78.243
7/7 0-24 (BL)	2014-02-01	2014-02-28	0.000	0.000
7/7 0-24 (BL)	2014-03-01	2014-03-31	-80.551	-80.551
7/7 0-24 (BL)	2014-01-01	2014-03-31	3.014	3.014
7/7 0-24 (BL)	2014-04-01	2014-06-30	20.133	20.133
7/7 0-24 (BL)	2014-07-01	2014-09-30	-37.922	-10.000
7/7 0-24 (BL)	2014-10-01	2014-12-31	0.000	0.000
7/7 0-24 (BL)	2014-01-01	2014-12-31	248.333	248.333

Comparison

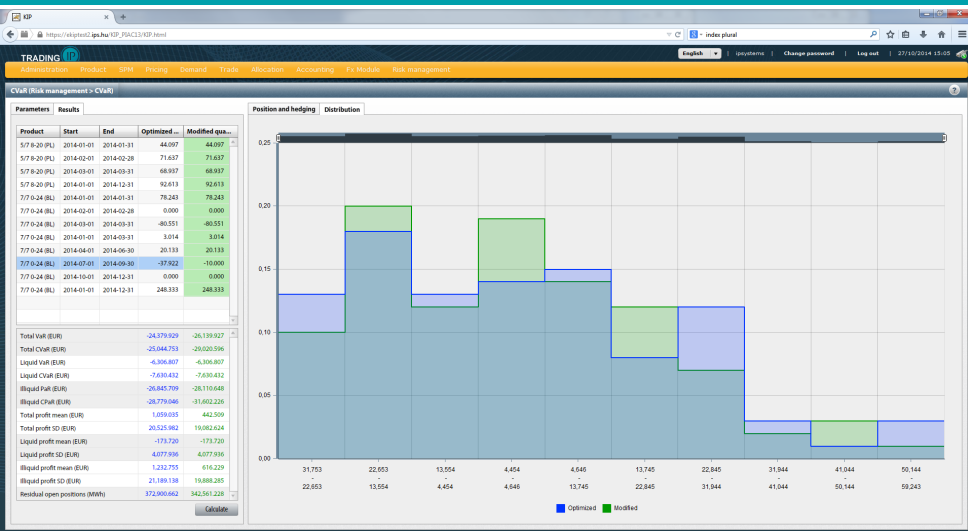


Comparison

Total VaR (EUR)	-24,379.929	-26,139.927
Total CVaR (EUR)	-25,044.753	-29,020.596
Liquid VaR (EUR)	-6,306.807	-6,306.807
Liquid CVaR (EUR)	-7,630.432	-7,630.432
Illiquid PaR (EUR)	-26,845.709	-28,110.648
Illiquid CPaR (EUR)	-28,779.046	-31,602.226
Total profit mean (EUR)	1,059.035	442.509
Total profit SD (EUR)	20,525.982	19,082.624
Liquid profit mean (EUR)	-173.720	-173.720
Liquid profit SD (EUR)	4,077.936	4,077.936
Illiquid profit mean (EUR)	1,232.755	616.229
Illiquid profit SD (EUR)	21,189.138	19,888.285
Residual open positions (MWh)	372,900.662	342,561.228

Calculate

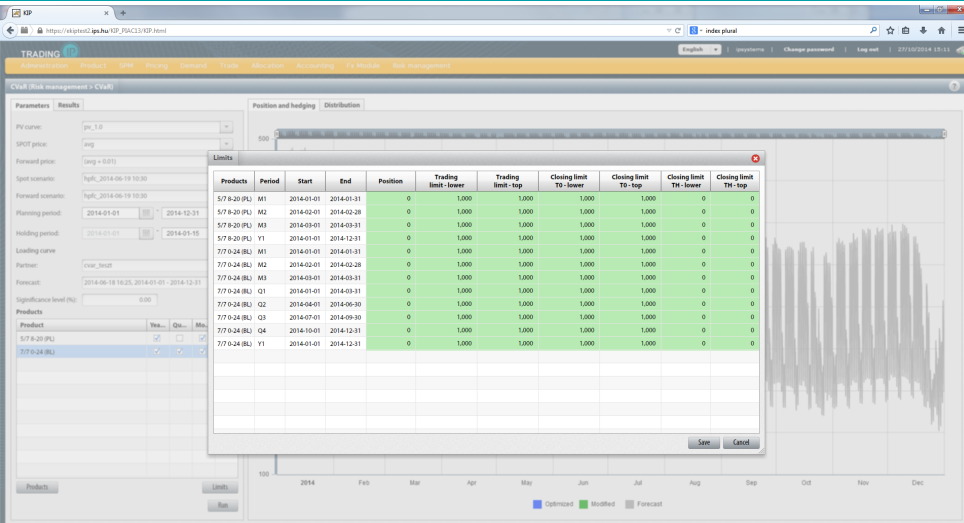
Comparison: histograms



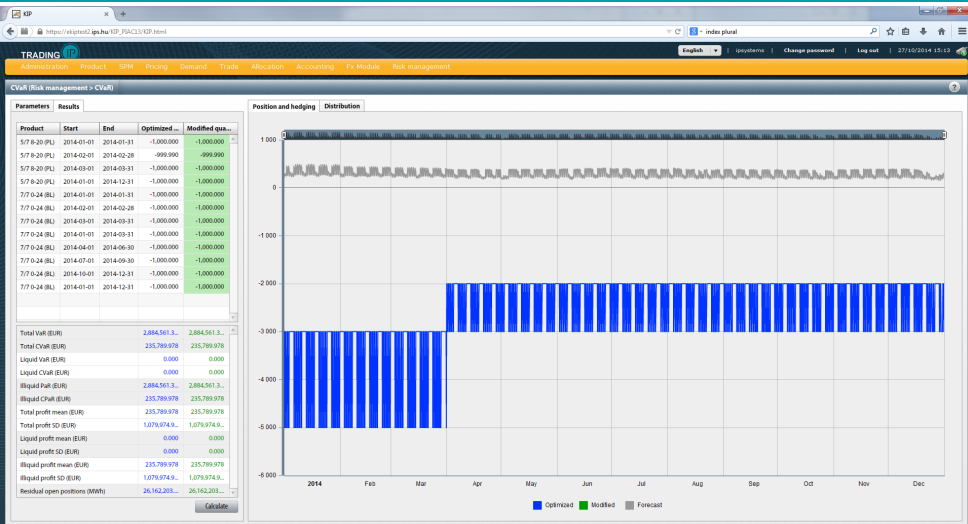
Expected value: zero level of significance

Parameters	Results			
PV curve:	pv_1.0			
SPOT price:	avg			
Forward price:	(avg + 0.01)			
Spot scenario:	hpfc_2014-06-19 10:30			
Forward scenario:	hpfc_2014-06-19 10:30			
Planning period:	2014-01-01 - 2014-12-31			
Holding period:	2014-01-01 - 2014-01-15			
Loading curve				
Partner:	cvar_teszt			
Forecast:	2014-06-18 16:25, 2014-01-01 - 2014-12-31			
Significance level (%):	0.00			
Products				
Product	Yea...	Qu...	Mo...	We...
5/7 8-20 (PL)	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>
7/7 0-24 (BL)	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>

Liquidity limits



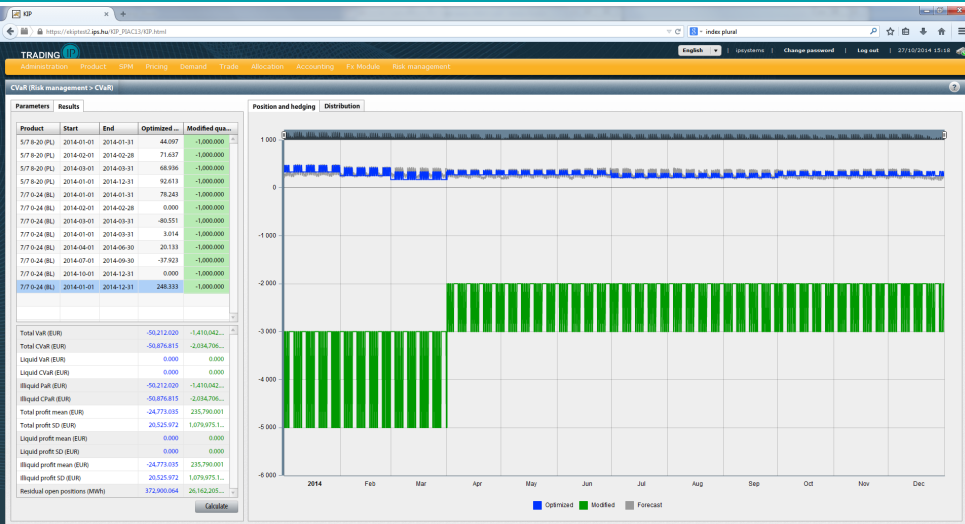
Result of expected value



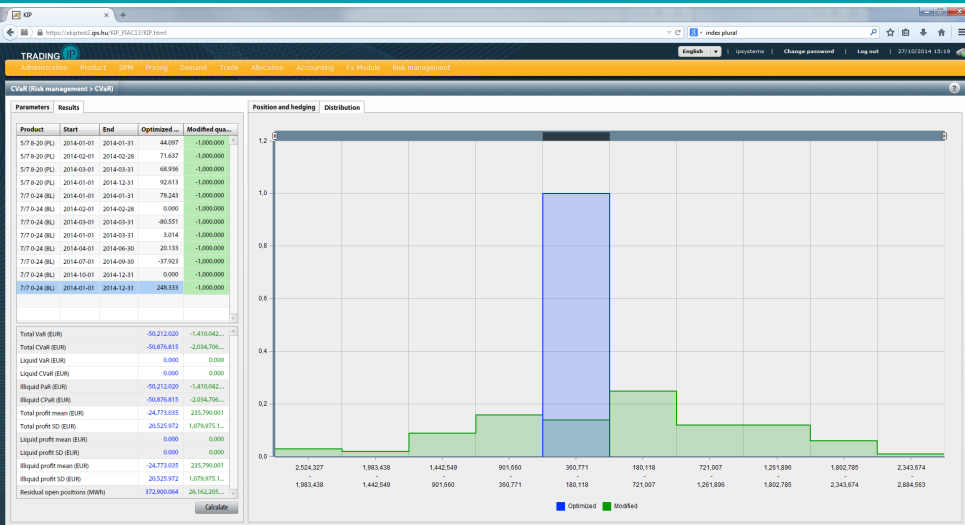
Result of CVaR at level of significance 95%



Comparison: residual open positions



Comparison: histograms



Benefits of CVaR

1. CVaR is a coherent risk measure.
(Subadditivity)
2. CVaR accounts for losses exceeding VaR.
(In the energy markets, the distribution of loss is usually non-normal and heavily tailed.)
3. CVaR is continuous in L .
4. CVaR is convex in L .
5. CVaR optimization can be reduced to convex programming and in some cases to linear programming.

Benefits of the application

1. In spite of the deterministic model, the risk of price moving is
 - ▶ managed and
 - ▶ measured exactly.
2. The tool supports both of the
 - ▶ traders/portfolio managers: instant risk information and support,
 - ▶ and risk managers/controllers: instant risk indices.
3. Usually, the risk manager measures the risk of open positions (typically by VaR or CVaR).
 - ▶ The liquidity reserve is calculated based on the risk indicator.
 - ▶ Based on the risk minimiser tool the traders are minimising the CVaR.
 - ▶ The CVaR is a coherent risk measure, hence the risk of the overall portfolio will be lower and the necessary liquidity reserve will decrease.