## Problems to the Laws of Large numbers

- 1. A fair dice is casted independently 600 times. Give an approximation (by CLT) for the probability that the number of 6's falls between 95 and 110.
- 2. *Elections 2000.* In a state (call it Florida) the voters vote for two candidates (with 0.5-0.5 probability), independently of each other. If there are 5 million voters, what is the probability that the difference of the votes given for the two candidates is less than 300 in absolute value.
- 3. 1000 person arrive to the left or right entrance of a theatre independently (they choose between the entrances with 0.5-0.5 probability). How many hangers to place into the left and right cloak rooms, if they want to give only a 1 percent chance to the event that somebody cannot place his/her coat in the nearest cloakroom. (Each pearson has a coat.)
- 4. Use the Weak Law of Large Numbers to prove that for the true probability p of an event and for its relative frequency  $\overline{X}_n$  based on an *n*-element i.i.d. Bernoully sample:

$$\mathbb{P}(|\overline{X}_n - p| \ge \varepsilon) \le \frac{p(1-p)}{n\varepsilon^2} \le \frac{1}{4n\varepsilon^2}, \qquad \forall \varepsilon > 0.$$

5. Opinion poll. On the basis of the previous exercise find the number n of people to be interviewed so that the true (but unknown) population support p of a candidate and its relative frequency based on this poll differ at most 0.01 with probability at least 90 percent.