

$$f_n(x) = 2^n \sqrt{1 - \left(\frac{x}{2}\right)^2}^n, \quad f_n(0) = 2^n, \quad \text{so let } u_n = \frac{1}{2^n}.$$

$$\text{Now } u_n f_n(x) = \sqrt{1 - \left(\frac{x}{2}\right)^2}^n$$

$$\text{and } \int_{-2}^2 u_n f_n(x) dx = \int_{-2}^2 \sqrt{1 - \left(\frac{x}{2}\right)^2}^n dx \xrightarrow[x=2d_y]{x=z} 2 \int_{-1}^1 \sqrt{1 - y^2}^n dy \quad \text{other HA } 2 \sqrt{\frac{2\pi}{n}}$$

$$\text{Now } \int u_n f_n(v_n x) dx \xrightarrow[x=\frac{1}{v_n} dz]{x=\frac{z}{v_n}} \int_{-2}^2 u_n f_n(z) \frac{1}{v_n} dz = \frac{1}{v_n} \int_{-2}^2 u_n f_n(z) dz$$

on its domain

$$\sim \frac{1}{v_n} 2 \sqrt{\frac{2\pi}{n}}$$

This converges to 1 iff $v_n \sim 2 \sqrt{\frac{2\pi}{n}}$

so let $v_n = 2 \sqrt{\frac{2\pi}{n}}$.

$$\text{Now } g_n(x) = u_n f_n(v_n x) = \sqrt{1 - \left(\frac{2 \sqrt{\frac{2\pi}{n}} x}{2}\right)^2}^n = \sqrt{\left(1 - \frac{2\pi x^2}{n}\right)^n}$$

Since $\left(1 + \frac{c}{n}\right)^n \rightarrow e^c$ for every $c \in \mathbb{R}$,

$$g_n(x) \rightarrow \sqrt{e^{-2\pi x^2}} = \underline{\underline{e^{-\pi x^2} = g(x)}}$$