

Self-similar finite  $p$ -groups  
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**Abstract:** In this talk, we address the following question: when is a finite  $p$ -group  $G$  self-similar, i.e. when can  $G$  be faithfully represented as a self-similar group of automorphisms of the  $p$ -adic tree? We show that, if  $G$  is a self-similar finite  $p$ -group of rank  $r$ , then its order is bounded by a function of  $p$  and  $r$ . This applies in particular to finite  $p$ -groups of a given coclass. In the particular case of groups of maximal class, that is, of coclass 1, we can fully answer the question above: a  $p$ -group of maximal class  $G$  is self-similar if and only if it contains an elementary abelian maximal subgroup over which  $G$  splits. Furthermore, in that case the order of  $G$  is at most  $p^{p+1}$ , and this bound is sharp.

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