# T H I R D E D I T I O N CALCULUS EARLY TRANSCENDENTALS 



BRIGGS
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## MyLab Math for Calculus: Early Transcendentals, 3e

(access code required)

Used by over 3 million students a year, MyLab™ Math is the world's leading online program for teaching and learning mathematics. MyLab Math for Calculus: Early Transcendentals, 3e delivers text-specific assessment, tutorials, and multimedia resources that provide engaging and personalized experiences, so learning can happen in any environment and course format.

## eBook with Interactive Figures

This groundbreaking eBook includes approximately 700 figures that can be manipulated to provide a deeper geometric understanding of key concepts. Plus, all-new Enhanced Interactive Figures incorporate functionality from several standard Interactive Figures, making each one mathematically richer and ideal for in-class demonstrations.


Compute the volume of the solid bounded by the planes below

$$
x=0, x=7, z=y-2, z=-4 y-2, z=0, z=2
$$

Find the double integral needed to determine the volume of the solid.
$\frac{5}{4} \int_{0}^{7} \int_{0}^{2}(z+2) d z d x$
The volume of the solid is $\frac{105}{2}$ cubic units. (Simplify your answer.)

## ALL NEW! Instructional Videos

For each section of the text, there is a newly recorded full-lecture video. Many videos make use of Interactive Figures to enhance understanding of concepts. To make them easier to navigate, each lecture video is segmented into parts (Introduction, Example, or Summary). The videos are assignable within MyLab Math, and a Guide to Video-Based Assignments shows which MyLab Math exercises correspond to each video.

## Questions that Deepen Understanding

 MyLab Math includes a variety of question types designed to help students succeed in the course. In Setup \& Solve questions, students show how they set up a problem as well as the solution, better mirroring what is required on tests. Additional Conceptual Questions were written by faculty at Cornell University to support deeper, theoretical understanding of the key concepts in calculus.

## ALGEBRA

## Exponents and Radicals

$x^{a} x^{b}=x^{a+b}$
$\frac{x^{a}}{x^{b}}=x^{a-b}$
$x^{-a}=\frac{1}{x^{a}}$
$\left(x^{a}\right)^{b}=x^{a b} \quad\left(\frac{x}{y}\right)^{a}=\frac{x^{a}}{y^{a}}$
$x^{1 / n}=\sqrt[n]{x}$
$x^{m / n}=\sqrt[n]{x^{m}}=(\sqrt[n]{x})^{m} \quad \sqrt[n]{x y}=\sqrt[n]{x} \sqrt[n]{y}$

## Factoring Formulas

$a^{2}-b^{2}=(a-b)(a+b) \quad a^{2}+b^{2}$ does not factor over real numbers. $a^{3}-b^{3}=(a-b)\left(a^{2}+a b+b^{2}\right) \quad a^{3}+b^{3}=(a+b)\left(a^{2}-a b+b^{2}\right)$ $a^{n}-b^{n}=(a-b)\left(a^{n-1}+a^{n-2} b+a^{n-3} b^{2}+\cdots+a b^{n-2}+b^{n-1}\right)$

## Binomial Theorem

$(a+b)^{n}=a^{n}+\binom{n}{1} a^{n-1} b+\binom{n}{2} a^{n-2} b^{2}+\cdots+\binom{n}{n-1} a b^{n-1}+b^{n}$, where $\binom{n}{k}=\frac{n(n-1)(n-2) \cdots(n-k+1)}{k(k-1)(k-2) \cdots 3 \cdot 2 \cdot 1}=\frac{n!}{k!(n-k)!}$

## Binomials

$$
\begin{aligned}
& (a \pm b)^{2}=a^{2} \pm 2 a b+b^{2} \\
& (a \pm b)^{3}=a^{3} \pm 3 a^{2} b+3 a b^{2} \pm b^{3}
\end{aligned}
$$

## Quadratic Formula

The solutions of $a x^{2}+b x+c=0$ are

$$
x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a} .
$$

## GEOMETRY



## TRIGONOMETRY


$\cos \theta=\frac{\text { adj }}{\text { hyp }} \sin \theta=\frac{\text { opp }}{\text { hyp }} \tan \theta=\frac{\text { opp }}{\text { adj }}$
$\sec \theta=\frac{\text { hyp }}{\operatorname{adj}} \quad \csc \theta=\frac{\text { hyp }}{\text { opp }} \quad \cot \theta=\frac{\text { adj }}{\text { opp }}$


$$
\begin{aligned}
\cos \theta=\frac{x}{r} & \sec \theta=\frac{r}{x} \\
\sin \theta=\frac{y}{r} & \csc \theta=\frac{r}{y} \\
\tan \theta=\frac{y}{x} & \cot \theta=\frac{x}{y}
\end{aligned}
$$



## Reciprocal Identities

$\tan \theta=\frac{\sin \theta}{\cos \theta} \quad \cot \theta=\frac{\cos \theta}{\sin \theta} \quad \sec \theta=\frac{1}{\cos \theta} \quad \csc \theta=\frac{1}{\sin \theta}$

## Pythagorean Identities

$\sin ^{2} \theta+\cos ^{2} \theta=1 \quad \tan ^{2} \theta+1=\sec ^{2} \theta \quad 1+\cot ^{2} \theta=\csc ^{2} \theta$

## Sign Identities

$\sin (-\theta)=-\sin \theta \quad \cos (-\theta)=\cos \theta \quad \tan (-\theta)=-\tan \theta$
$\csc (-\theta)=-\csc \theta \quad \sec (-\theta)=\sec \theta \quad \cot (-\theta)=-\cot \theta$

## Double-Angle Identities

$$
\begin{array}{rlrl}
\sin 2 \theta & =2 \sin \theta \cos \theta & \cos 2 \theta & =\cos ^{2} \theta-\sin ^{2} \theta \\
& & =2 \cos ^{2} \theta-1 \\
\tan 2 \theta & =\frac{2 \tan \theta}{1-\tan ^{2} \theta} & & =1-2 \sin ^{2} \theta
\end{array}
$$

## Half-Angle Identities

$\cos ^{2} \theta=\frac{1+\cos 2 \theta}{2} \quad \sin ^{2} \theta=\frac{1-\cos 2 \theta}{2}$

## Addition Formulas

$\sin (\alpha+\beta)=\sin \alpha \cos \beta+\cos \alpha \sin \beta$
$\cos (\alpha+\beta)=\cos \alpha \cos \beta-\sin \alpha \sin \beta$
$\tan (\alpha+\beta)=\frac{\tan \alpha+\tan \beta}{1-\tan \alpha \tan \beta}$
$\sin (\alpha-\beta)=\sin \alpha \cos \beta-\cos \alpha \sin \beta$
$\cos (\alpha-\beta)=\cos \alpha \cos \beta+\sin \alpha \sin \beta$
$\tan (\alpha-\beta)=\frac{\tan \alpha-\tan \beta}{1+\tan \alpha \tan \beta}$

Law of Sines
$\frac{\sin \alpha}{a}=\frac{\sin \beta}{b}=\frac{\sin \gamma}{c}$


## Law of Cosines

$a^{2}=b^{2}+c^{2}-2 b c \cos \alpha$

## Graphs of Trigonometric Functions and Their Inverses



# Calculus EARLY TRANSCENDENTALS 

Third Edition

WILLIAM BRIGGS<br>University of Colorado, Denver

LYLE COCHRAN<br>Whitworth University

## BERNARD GILLETT

University of Colorado, Boulder

## ERIC SCHULZ

Walla Walla Community College

Director, Portfolio Management:<br>Executive Editor:<br>Content Producer:<br>Managing Producer: Producer:<br>Manager, Courseware QA:<br>Manager, Content Development:<br>Product Marketing Manager:<br>Field Marketing Manager:<br>Marketing Assistants:<br>Senior Author Support/Technology Specialist:<br>Manager, Rights and Permissions:<br>Manufacturing Buyer:<br>Text and Cover Design, Production<br>Coordination, Composition:<br>Illustrations:<br>Cover Image:

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