## 1. LOCAL ERGODICITY

### 1.1. **Semi-dispersing billiards.**

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## 2. ERGODICITY

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## 3. Correlation decay and CLT

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