## **FUNCTIONAL ANALYSIS 1**

- 1. Metric spaces. Compact set, sequentially compact set, totally bounded set. Relative compact set. Arzela-Ascoli theorem.
- 2. Normed spaces, Banach spaces. Series in normed spaces. Finite dimensional normed spaces.
- 3. Linear operators on normed spaces. Boundedness and continuity. The normed space of bounded linear operators.
- 4. Baires theorem. The principle of uniform boundedness. Banach-Steinhaus theorems.
- 5. The open mapping theorem, Banachs theorem on the bounded inverse, closed graph theorem.
- 6. Linear functionals and dual spaces. Hahn-Banach extension theorems, Hahn-Banach separation theorems. Reflexivity.
- 7. Weak convergence, weak \*-convergence. Banach-Alaoglu theorem. theorem.
- 8. Compact operators, Schauders theorem.
- 9. The spectrum of a bounded linear operator. Neumann series, the resolvent. The spectral radius formula. The spectrum of a compact operator.
- 10. Inner product spaces. Projection theorem. Orthonormal bases. Riesz-Fischer theorem.
- 11. Rieszs representation theorem, the Hilbert space adjoint of a bounded linear operator.
- 12. The spectral theorem for normal compact operators.